

Review for Exam 3

Class Weeks, topics and dates	Book Chapters	Lab numbers and Topics
Week 1 1D motion and units 1/17	Ch.1.1-6 and 2	Introduction
Week 2 2D motion , vectors 1/23	Ch. 1.7-9 and 3.1-3	109. 1 D motion
Week 3 Forces + exam 1 review; 1/30	Ch. 4	111. Projectile motion
Exam 1 1D&2D motion, units,vectors; 2/6	On Weeks 1-2	
Week 4 Linear static forces 2/6	Ch. 5.1 and 11	112 Newton's 2nd
Week 5 Friction 2/13	Ch. 5.2-3	103 Linear statics
Week 6 Work and Kinetic Energy 2/20	Ch. 1.10 and 6	106 Friction
Week 7 Potential and conservation of Energy + exam 2 review 2/27	Ch. 7	New: Work and Kinetic Energy
Exam 2 Forces, friction, energy 3/6	On weeks 3-6	
Week 8 Momentum and Collisions 3/6	Ch. 8	125 Conservation of Energy
Spring break 3/13		
Week 9 Circular motion 3/20	Ch. 3.4 and 5.4	126 Conservation of momentum
Week 10 Torque, Moment of Inertia 3/27	Ch. 1.10 and 9	114 Circular motion
Week 11 Rotational Motion 4/3	Ch. 10.1-6	127 Torque and rotation
Exam 3 on conservation, circular motion & torque 4/10	On weeks 7-11	
Week 12 Rotation statics+Exam 3 rev. 4/10	Ch. 11.1-3	120 Conservation angular energy
Week 13 Fluid Mechanics 4/17	Ch. 12.1-5	121 rotation static forces
Week 14 Universal Gravitation 4/24	Chap. 13	7 Archimedes' Principle
Review of the course 5/1		
Classes end 5/2		
Final exam tbd	Weeks 1-14	

Wheel slows down

A wheel decelerates at a rate of 0.3 Radians/s^2 It turns 50 times and then stops. Long does it take?

$$\alpha = (\omega - \omega_0) / t$$
$$= -0.3 \text{ m/s}^2$$

$$\omega_{\text{ave}} = 2\pi \cdot 50 / t = \omega_0 / 2$$

$$\omega_0 = 628 / t$$

$$-0.3 = (0 - 630 / t) / t$$

$$t = \sqrt{630 / .3} = 45 \text{ s}$$

Rolling ring

A disk rolls straight down a hill and is going 8 m/s at the bottom. How high is the hill?

$$mgh = mv^2/2 + I\omega^2/2$$

$$I = mR^2/2; \omega = v/R \Rightarrow I\omega^2 = .5mR^2v^2/R^2$$

$$mgh = mv^2/2 + mv^2/4 = mv^2(3/4)$$

$$h = (1/g)v^2(3/4) = (1/9.8)(64)(3/4) = 5$$

Yoyo

A person holds one end of a string and the other end is wound around a disk. The initial angular acceleration of the disk is 130 radians/s^2 . What is the radius of the disk?

$$mg - F = ma$$

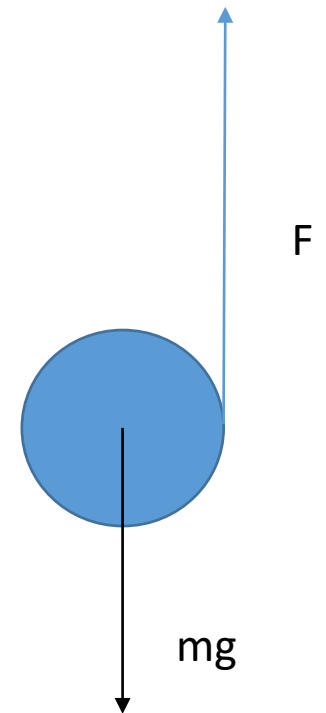
$$\text{Torque} = FR = I \alpha = .5 m R^2 a / R$$

$$F = .5ma$$

$$mg - .5ma = ma$$

$$g = 1.5a = 1.5\alpha R$$

$$R = g / 1.5\alpha = 9.8 / (1.5 * 130) = 0.05 \text{ m}$$



Falling elevator

An elevator falls without friction. It's mass is 2000kg, the counter weight is 1900 kg and the pulley is a disk of mass 400 kg and radius 2 m. When it hits, its speed is 2 m/s. How far did it fall?

$$(M-m)gh = \frac{1}{2} (M+m) v^2 + \frac{1}{2} I \omega^2$$

$$I = \frac{1}{2} M' R^2; \quad \omega = v/R$$

$$(M-m)gh = \frac{1}{2} (M+m) v^2 + \frac{1}{4} M' v^2$$

$$h = \frac{1}{2} (v^2) (M+m + M'/2) / g(M-m)$$

$$= .5 * 4 * (2000 + 1900 + 400/2) / 9.8 * (100)$$

$$= 8$$

Conservation of momentum

- A ring that is dropped on a rotating cylindrical table. The ring is centered on the table and oriented with the same axis as the table. The ring has a moment of inertia of $0.04\text{kg}\cdot\text{m}^2$. The ring is initially not rotating and the table is rotating at 15 radians/s . The table has a radius of 0.33m and the velocity of a point on the edge of the table is 1.0 m/s after the drop? What is the moment of inertia of the table?
 - a. 0.10
 - b. 0.56
 - c. 0.24
 - d. 0.03
 - e. 0.01

Momentum: Table+0= both

$$I_t * \omega_t + 0 = (I_t + I_r) * \omega$$

$$I_t = I_r * \omega / (\omega_t - \omega)$$

Also need: $\omega = v/R = 1/.33 = 3$

$$I_t = 0.04 * 3 / (15 - 3) = 0.01$$

1. Linear and angular acceleration

- A merry-go-round (a disk) is accelerating at 3 Radians/s². A woman feels a linear acceleration of 15 m/s². How far from the center is she standing?
- $a = \alpha r \Rightarrow r = 15/3 = 5$

Angular acceleration

- A disk starts from rest and speeds up to an angular velocity of 3 radians/s in 30 s. What is its angular acceleration?
- $\alpha = \omega/t \Rightarrow 3/30 = 0.1$ radians/s²

Moment of inertia

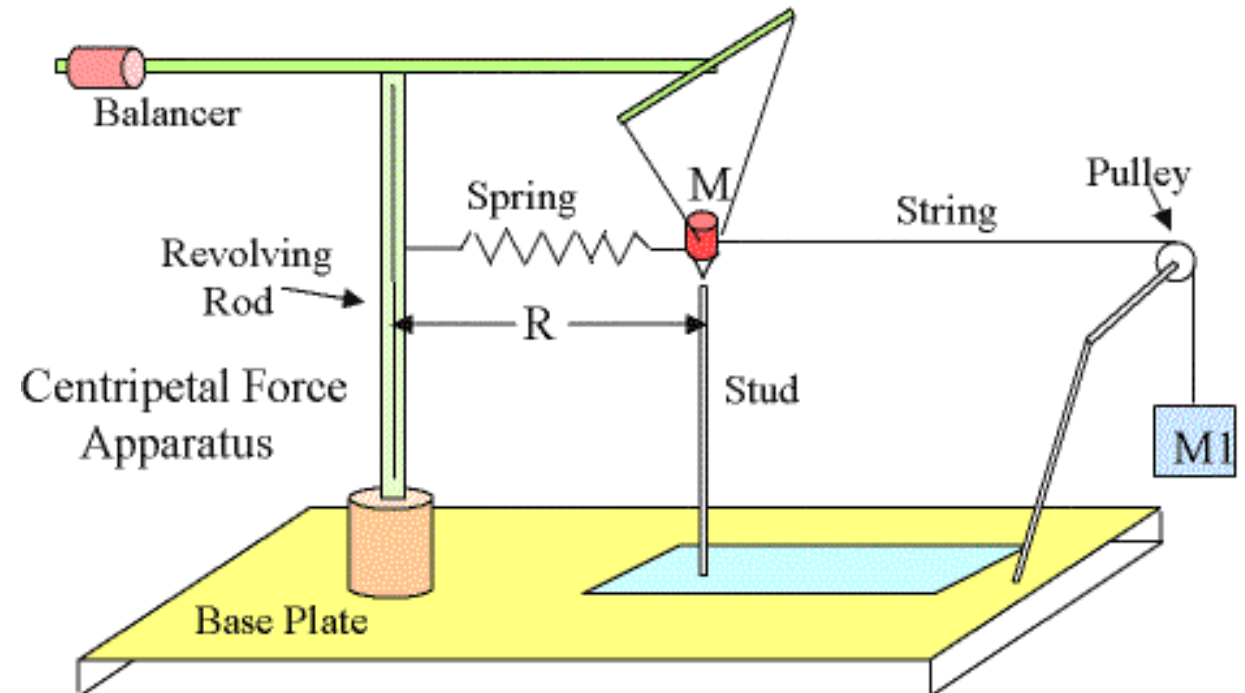
- A disk is rotating around its center axis. The moment of inertia of the disk is 32 kg m^2 . The mass of the disk is 4kg . What is the radius?
- $I = \frac{mr^2}{2} \Rightarrow r^2 = \frac{2I}{m} \Rightarrow r = 4$

R of rotation

As in the lab, 0.1kg mass is held by a spring . It is rotating at an angular velocity of 10 radians/s. Its linear velocity is 1m/s. What is the length of the spring in m?

- a. 1
- b. 10
- c. .01
- d. 100
- e. 0.1

$$v = \omega R$$
$$R = v / \omega$$
$$= 0.1 \text{m}$$

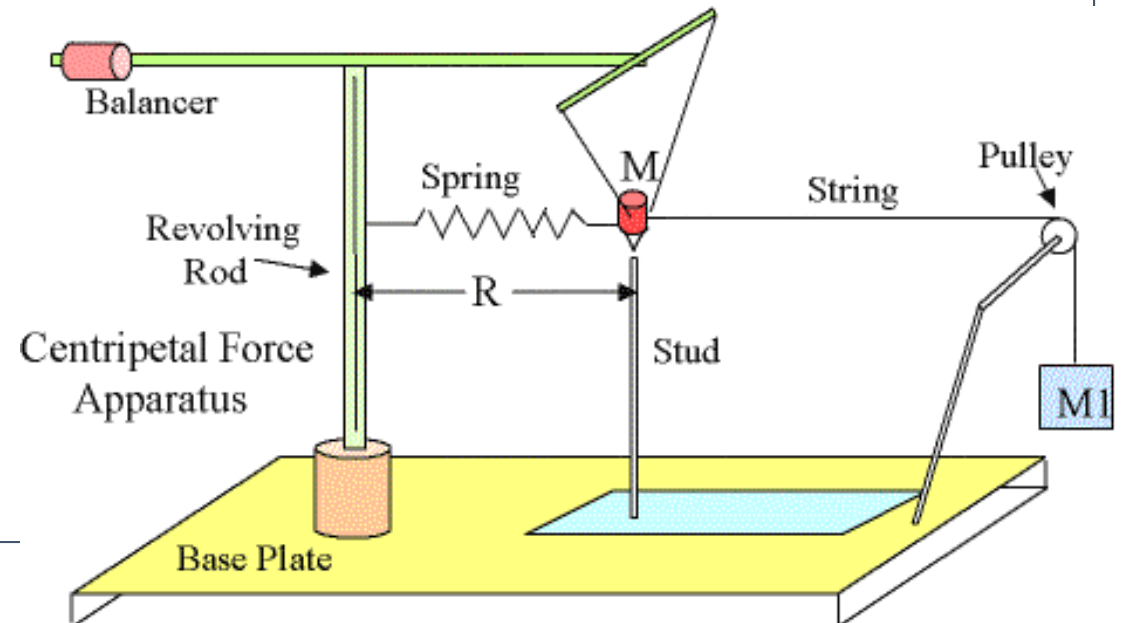


Mass in rotation

- As in the lab, a revolving object is held with a spring. You adjust the radius of rotation to 0.05m. The force on the spring is 0.5N. The linear velocity is 1.6m/s. What is the mass of the weight?

- a. 0.02
- b. 0.01
- c. 0.5
- d. 0.25
- e. 0.008

$$\begin{aligned} F &= ma \\ a &= v^2/R \\ m &= RF/v^2 \\ &= 0.01 \end{aligned}$$

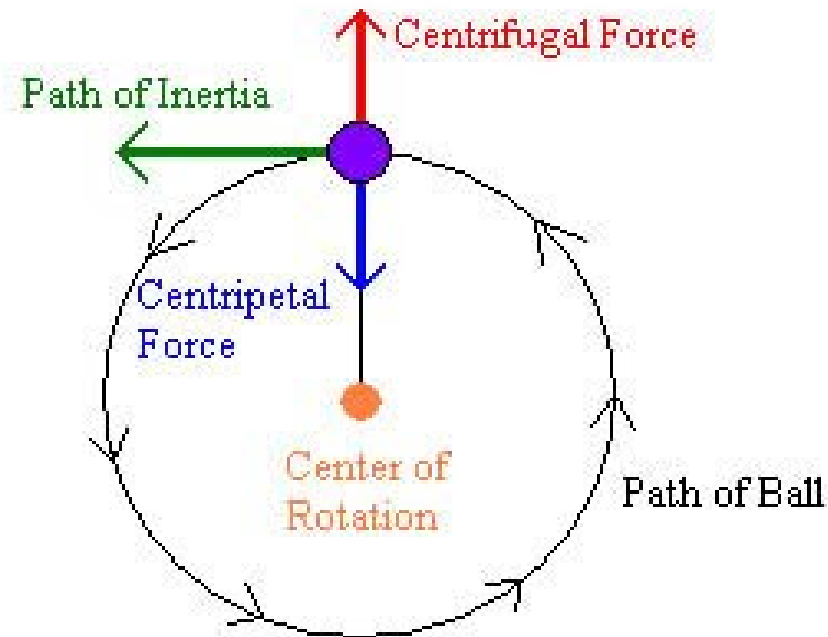


Acceleration in rotation

A mass of 50kg is rotating on a string with a radius of 0.5m and a number of rotations/s of 0.5. What is the centripetal acceleration of the mass?

- a. 9.8
- b. 2.4
- c. 4.9
- d. 1.2
- e. 10.2

$a = v^2/R$
$v = 2\pi r \nu$
$a = 4.9$



Inelastic collision

A car of mass $1/5$ kg is moving at a velocity $+1/4$ m/s. It hits a car head on of mass 0.1 kg and velocity -0.5 m/s. They stick together. How fast (in m/s) is the wreck moving just after the collision.

- a. 0.25
- b. -0.1
- c. -0.5
- d. +0.1
- e. 0

$$m_1v_1+m_2v_2=(m_1+m_2)*V$$
$$.2*.25-.1*.5=0$$

Explosion

Two cars are connected by a compressed spring. The spring is released. The car with mass 0.2kg shoots off with velocity 5m/s. The other car goes off with velocity -0.1 m/s. What is the mass (in kg) of the slow car?

- a. 5
- b. 10
- c. 0.1
- d. 1
- e. 0

$$\begin{aligned}0 &= m_1 \cdot v_1 + m_2 \cdot v_2 \\ m_2 &= -m_1 \cdot v_1 / v_2 \\ &= 0.2 \cdot 5 / .1 = 10\end{aligned}$$

Dart into toy car

A dart is fired at a speed of 500m/s into a stationary toy car with mass 3.5 kg, on a frictionless, horizontal rail. After the collision, the dart sticks in the car and they move together at 1 m/s. Find the mass of the dart, in kg.

- a. 5/100
- b. 7/100
- c. 2/1000
- d. 3.5/1000
- e. 7/1000

$$\begin{aligned}mV &= (M+m)v \\ m &= (M+m)v/V = (3.5) * 1/500 \\ &= 3.5/500 = 7/1000\end{aligned}$$

Impulse of a glider

A glider of mass 5kg and velocity +2m/s hits the end of a horizontal rail and bounces off in the opposite direction. The collision is inelastic with an average force of -100N and a duration of 0.2 s. What is the final velocity (in m/s)?

- a. -22
- b. 22
- c. -20
- d. -2
- e. -6

$$\begin{aligned}mv' - mv &= Ft \\mv' &= Ft + mv \\v' &= Ft/m + v \\&= -100 * 0.2 / 5 + 2 \\&= -2\end{aligned}$$

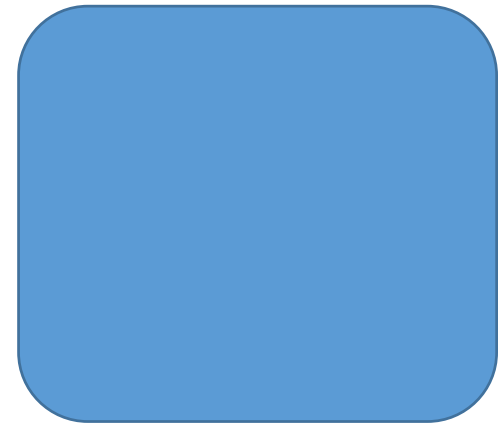
Center of mass

3 children are standing on a platform:

1. $m=40$ kg; $R=10i+2j$ m
2. $m=50$ kg; $R=-2i+3j$ m
3. $m=60$ kg; $R=3i + -4j$ m

Where R is relative to the center.

Where is the center of mass of the children?



Impulse of a bullet

A bullet is fired at a speed of 500m/s into a stationary block with mass 5kg, on a frictionless, horizontal surface. After the collision, the bullet gets stuck in the block and they move together at 1 m/s. The mass of the bullet is 0.01 kg. How big is the impulse (in N s) ?

- a. 500
- b. 0.01
- c. -500
- d. -.01
- e. -5

$$\begin{aligned}(M+m)v-mV &= Ft \\ Ft &= (5+.01)*1 - (0.01)*500 \\ &= -4.99\end{aligned}$$